



The Carnot-Method

for the Allocation of Input Factors on Multiple Energetic Co-Products

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Agenda

- Combined Production's Cost Calculation
- Allocation for Energetic Co-Products
- Exergetic Allocaton – the Carnot Method
- Figure: Primary Energy Factor for the Heat
- Examples for Exergy Balances



Cost Calculation with Combined Production

- CHP unit as cost center determining product features of Heat & Power
 - Monetary in € (variable costs)
 - Energetic in $\text{kWh}_{\text{INPUT}}$ per $\text{kWh}_{\text{OUTPUT}}$ (primary energy factor)
 - Environmental in $\text{g}_{\text{CO}_2\text{e}}/\text{kWh}$ (emission factor)
- Problem: How to allocate incoming variable costs on both co-products: electrical energy and useful heat
- Relevance
 - Heating bills for residential buildings
 - Calculation of variable production costs for large CHP plants
- Known methods such as
 - Substitution method
 - Equivalent parameter method
 - Disadvantages: external reference needed, variable at will
- BUT: Energetic co-products follow the rules of thermodynamics and can be transformed into each other

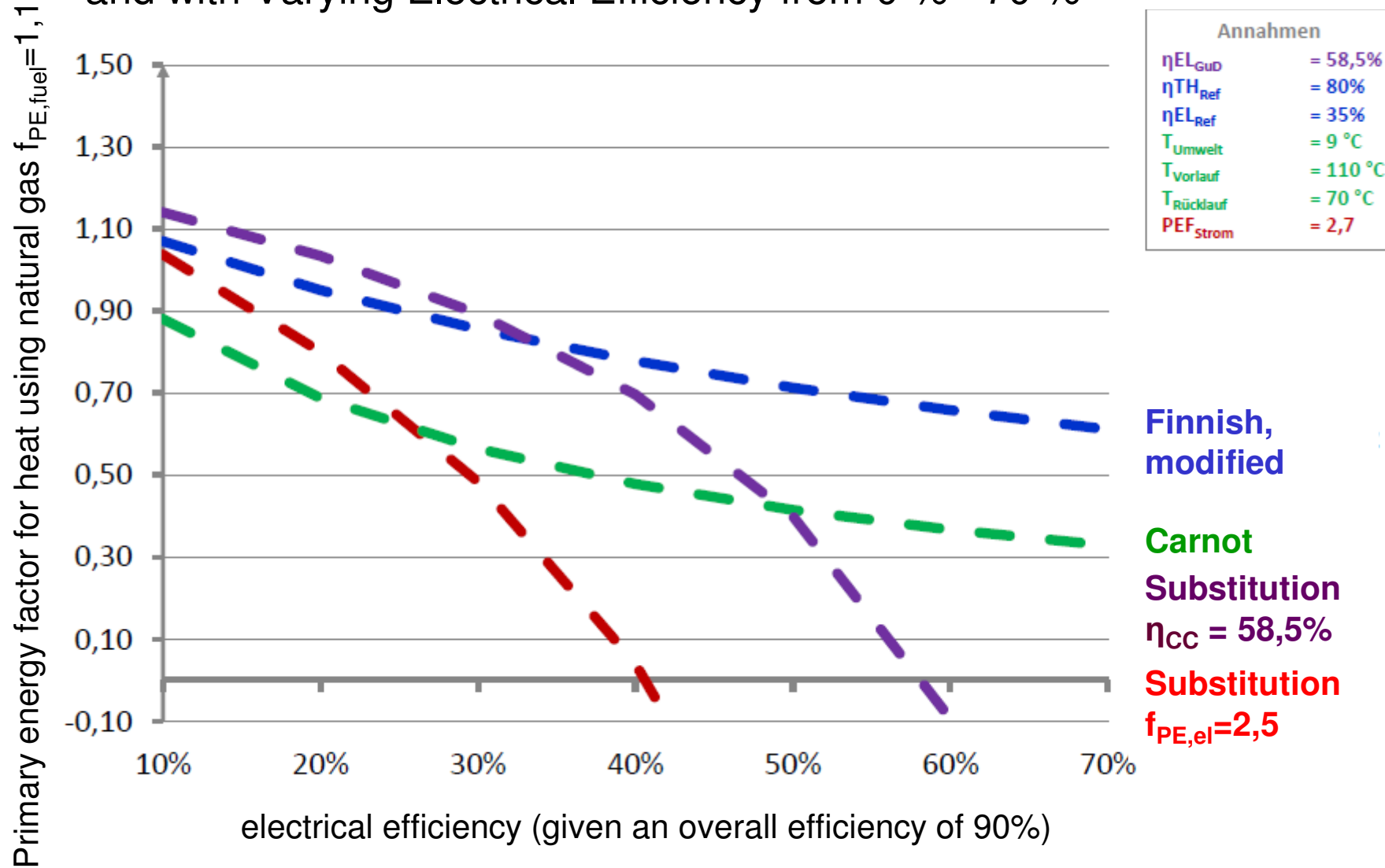
Allocation for Energetic Co-Products

- First Law: Conservation of Energy
- Energy goes In = Energy goes Out
 - $f_{\text{fuel}} \times Q_{\text{fuel}} = f_{\text{el}} \times P_{\text{el}} + f_{\text{th}} \times P_{\text{th}}$
 - Equation with two **unknown** variables as weighting factor
- Second equation is needed
 - Substitution method: external reference value for the by-product
 - Equivalent parameter: eg. energy content with $\text{kWh}_{\text{th}} = \text{kWh}_{\text{el}}$
 - **Or:**
- Second Law: Carnot's efficiency for transforming el \leftrightarrow th
 - $\eta_c \times P_{\text{th}}(T_s) = P_{\text{el}}$
 - $\eta_c = 1 - T_i/T_s$ depending of the ambient temperature T_i
and the useful heat P_{th} at level T_s

Exergetic Allocation – The Carnot Method

- Allocation of fuel input according to exergy content of energy output
- Carnot factor for the assessment of useful heat: $\eta_c = 1 - T_i/T_s$
describes the exchange value of heat and electricity
- Primary energy factors for heat and electricity:
 - $f_{PE,th} = (\eta_{th} \times \eta_c) / (\eta_{th} \times \eta_c + \eta_{el}) \times f_{PE,fuel}$
 - $f_{PE,el} = \eta_{el} / (\eta_{th} \times \eta_c + \eta_{el}) \times f_{PE,fuel}$
- Allocation without the need of external reference system
 - only unit parameters are needed η_{el} , η_{th} and T of heat output
- Example for a fuel cell ($\eta_{el} = 40\%$, $\eta_{th} = 40\%$)
 - $f_{PE,el} = \sim 2,0$ and $f_{PE,th} = \sim 0,5$
 - Efficiency of the virtual generator 50 %
 - Efficiency of the virtual boiler 200 %
- Exergetic efficiency as important quality feature for energy transformation

Primary Energy Factor for useful Heat at 90 % Overall Efficiency and with Varying Electrical Efficiency from 0 % - 70 %



Quelle: IFEU, Richtvert

Exergy – what is that exactly?

- Exergy: „valuable share of energy“
- Electrical and chemical energy: exergy content = 1
- Useful work which can be done by thermal energy $W = \eta_c \times Q$

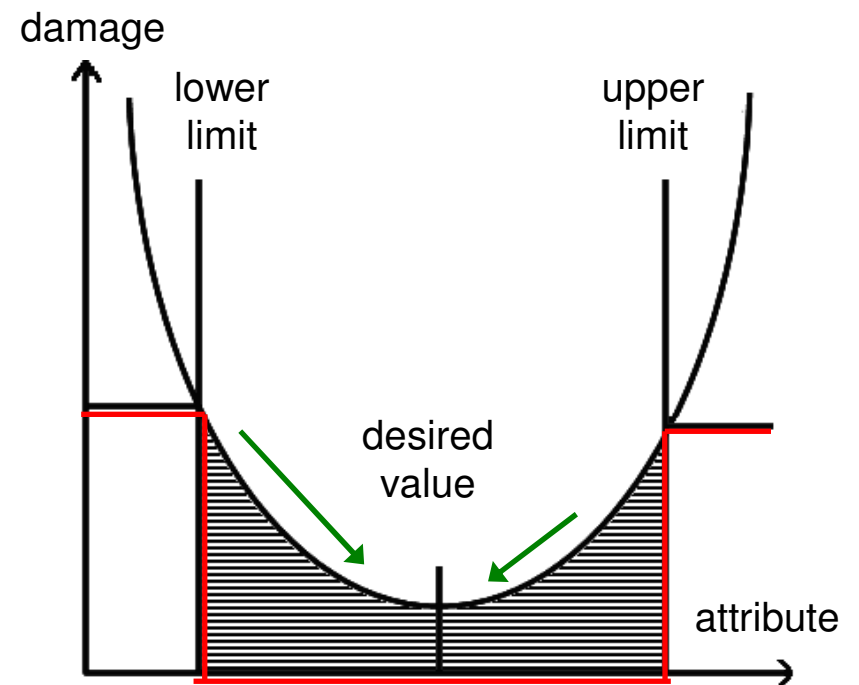
- From energy to exergy savings?
- Exergy based labelling for CHP units?

- Examples for energy transformation (X: exergy unit, $T_i=0^\circ\text{C}$)
 - Mini CHP unit (~20 kW): $100 X \rightarrow 30 X + 60 * 0,25 X = 45 X$
 - Boiler (90 °C): $100 X \rightarrow 100 * 0,25 X = 25 X$

 - Large CC w/h CHP: $100 X \rightarrow 60 X$
 - Heat pump (50 °C): $100 X \rightarrow 400 * 0,15 X = 60 X$
 - Power-to-Gas: $100 X \rightarrow 60 X$

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Genichi Taguchi's
quality assessment function